

# **AGRODEP Training Session**

## **“Poverty measurement and analysis”**

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## **Session 6**

# **Pro-poor growth**

# Content

Notions of pro-poor growth

The pro-poor growth measurement toolkit

The 'Non-anonymous approach'

## [ outline ]

Notions of pro-poor growth

The pro-poor growth measurement toolkit

The 'Non-anonymous approach'

# The issue

Does economic growth benefit the poor? If yes, by how much? How to assess the 'pro-poorness' of growth?

Technically, this is a normative evaluation of the change in the income (or expenditure or welfare) distribution from one period  $F_0$  to another  $F_1$ ,  $W(\Delta_F)$ .

Assessment on the basis of

- ▶ summary indicators
- ▶ graphical tools

## Differing views...

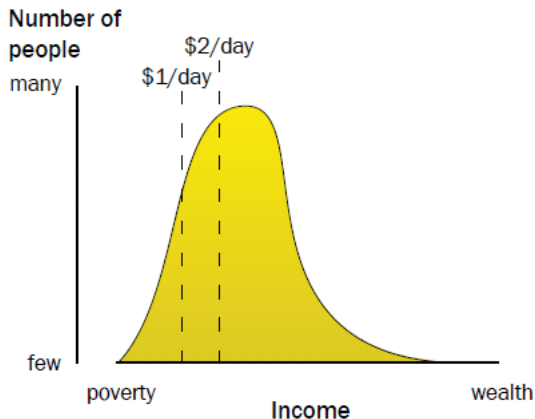
Relatively abundant recent methodological literature: see Kakwani & Pernia (2000), Ravallion & Chen (2003), Son (2004), Kakwani & Son (2008), Duclos (2009), Essama-Nssah & Lambert (2009)

But discussion of baseline definition of **what is pro-poor growth?** remains unclear (at least IMHO!)

Literature refers to

- ▶ So-called '**absolute perspective**': growth is said to be 'pro-poor' if economic growth goes with poverty reduction (often linked to Ravallion & Chen, 2003)
  - ▶ closely linked to poverty reduction targets
- ▶ So-called '**relative perspective**': growth is said to be 'pro-poor' if incomes of the poor grow proportionately more than for the non-poor
  - ▶ closely linked to inequality reduction targets

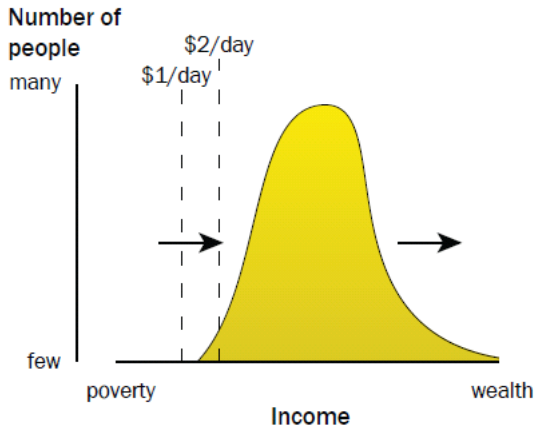
## Absolute or relative?



**Income distribution in a developing country with a large incidence of poverty**  
Wealth is very unevenly distributed, with many people struggling with low income.

# Absolute or relative?

## The absolute case

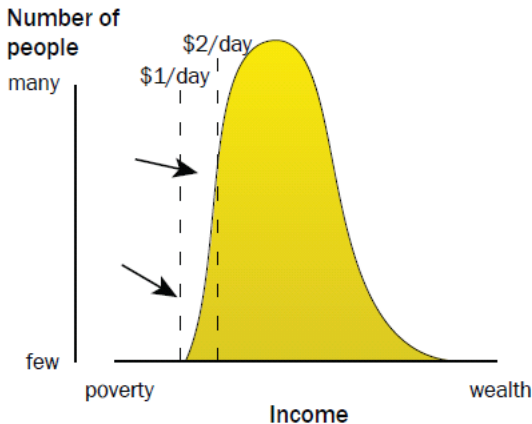


### Pro-poor growth, Absolute definition

The poor benefit from growth in the economy, and no consideration is given to the income distribution.

# Absolute or relative?

## The relative case



### Pro-poor growth, Relative definition

Through targeted strategic efforts, the growth in economy among the poor has a higher growth rate than the rest of the economy, thus changing the income distribution.

## Differing views...

But some commentators have argued that none of these two views are satisfactory *per se* and that, in effect, they should be observed jointly: to be labelled 'pro-poor', growth should reduce levels of poverty *and* be biased towards the poor compared to the non-poor (Osmani 2005)

Alone, none of the so-called 'absolute' and 'relative' perspectives are sufficient:

- ▶ this is obvious for the absolute perspective
- ▶ this becomes obvious for the relative perspective when growth is negative (in which case the absolute perspective is stronger!)

## A unified view: Benchmarking poverty change

A more fruitful point of departure in the recent literature involves contrasting poverty change against an explicit benchmark (Kakwani & Son (2008), Essama-Nssah & Lambert (2009), Duclos (2009)):

Growth (or recession) is said to be pro-poor if poverty falls more than in a **reference scenario**

- ▶ Kakwani & Son (2008), Essama-Nssah & Lambert (2009) advocate a reference scenario of equi-proportionate growth to all incomes calibrated to the change in mean income (but note that other standards could be specified)
- ▶ Duclos (2009) discusses both equi-proportionate growth and equal-additions as baseline (note how strong can be the latter)

## A unified view: Benchmarking poverty change (ctd.)

- ▶ The 'absolute perspective' corresponds to calibrating proportionate growth to 1 or equal additions to 0
- ▶ Beware that terminology is potentially confusing: The 'absolute perspective' is quite different from Duclos (2009)'s absolute, equal-additions benchmark!
  - ▶ Equal additions benchmark can be determined with reference to non-poor incomes (e.g., average income gains)
  - ▶ Equi-proportionate benchmark need not be set with reference to non-poor incomes
  - ▶ A benchmark combining the two classic perspectives is, e.g., an equi-proportionate growth of  $\max\left(1, \frac{\mu_1}{\mu_0}\right)$
- ▶ To me, **key distinction is whether benchmark is 'internal' or 'external'**

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## Growth incidence curves

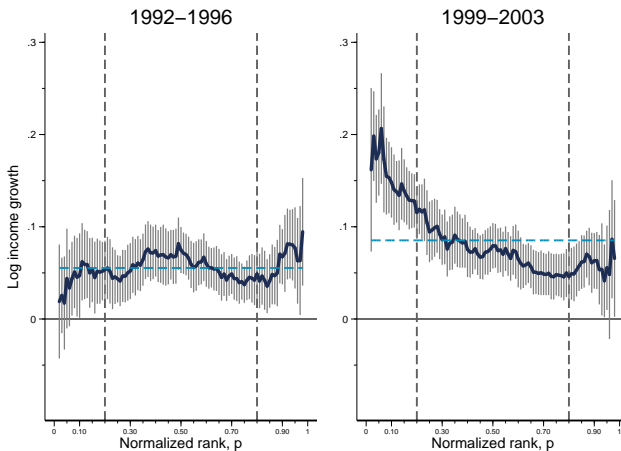
The growth incidence curve (GIC) traces the relative change of percentiles

$$g(p) = \frac{F_1^{-1}(p)}{F_0^{-1}(p)} - 1$$

against  $p \in (0, 1)$  (Ravallion & Chen, 2003).

R&C suggest from the GIC the 'rate of pro-poor growth'  $\frac{1}{H_0} \int_0^z g(p) dp$  as a summary index of pro-poor growth. It is the relative growth of income of the poor. It is also the change in the Watts poverty index divided by the initial headcount ratio.

## Growth incidence curves (ctd.)



## Growth incidence curves (ctd.)

$g(p) > 0$  for  $p < H_0$  is equivalent to first-order poverty dominance: poverty is reduced for a broad class of measures – pro-poor growth in ‘absolute sense’

(note that for a specific poverty index, dominance is not a necessary condition for pro-poor growth.)

$g(p) > \lambda$  for  $p < H_0$ , where  $\lambda = \frac{\mu_1}{\mu_0} - 1$  is interpreted as pro-poor growth in a ‘relative sense’.

## Poverty growth curves

A closely related graph is the poverty growth curve (PGC) which traces the relative change of incomplete means up to  $p$  – it is simply the area under the GIC curve up to point  $p$  divided by  $p$  (Son, 2004)

$$c(p) = \int_0^p \left( \frac{F_1^{-1}(s)}{F_0^{-1}(s)} - 1 \right) ds$$

against  $p \in (0, 1)$

## Poverty growth curves (ctd.)

$c(p) > 0$  for  $p < H_0$  is equivalent to second-order poverty dominance: poverty is reduced for a broad class of measures – pro-poor growth in ‘absolute sense’ (but again, for a specific poverty index, dominance is not a necessary condition for pro-poor growth.)

$c(p) > \lambda$  for  $p < H_0$ , where  $\lambda = \frac{\mu_1}{\mu_0} - 1$  is interpreted as pro-poor growth in a relative sense

## Essama-Nssah & Lambert (2008) measures

Interest in assessing 'pro-poorness' for a particular additive poverty measure of the type

$$P = \int_0^z \theta(y, z) f(y) dy$$

(with  $\theta(y, z)$  continuous, decreasing and convex in  $y$  being individual poverty 'contributions')

Growth is declared 'pro-poor' if observed poverty reduction in  $P$  is larger than reduction that would have been observed if growth had been equi-proportionate.

this approach encompasses several earlier indices, e.g., Kakwani & Pernia (2000)

## Essama-Nssah & Lambert (2008) measures (ctd.)

Building block:  $\phi_P$  the growth elasticity of  $P$  (i.e., percentage reduction in  $P$  for a 1 percent increase in mean income)

$$\phi_P(q) = \frac{1}{P} \int_0^{F(z)} y(p) \theta'(y(p), z) q(y(p)) dp$$

where  $y(p)$  is the  $p$ th quantile and  $q(y(p))$  is the GIC curve at  $p$  divided by the average growth rate (EN&L call it a 'growth pattern')

## Essama-Nssah & Lambert (2008) measures (ctd.)

Counterfactual: what would have been this elasticity with a flat growth pattern (which corresponds to the case of equal proportionate growth,  $q(y(p)) = 1$ )

$$\phi_P(q_0) = \frac{1}{P} \int_0^{F(z)} y(p) \theta'(y(p), z) dp$$

Pro-poor growth indices: excess reduction of poverty from  $q$  compared to reference

$$\pi_P(q) = P(\phi_P(q_0) - \phi_P(q))$$

$$\kappa_P(q) = \frac{\phi_P(q)}{\phi_P(q_0)}$$

## Essama-Nssah & Lambert (2008) measures (ctd.)

### Decomposition by source

Growth patterns can be expressed as functions of patterns within income sources:

$$q(y) = \sum_{j=1}^J \alpha_j(y) q_j(y)$$

where  $\alpha_j(y)$  is the share of income source  $j$  in total income at  $y$  and  $q_j(y)$  is the relative growth of component  $j$  at total income  $y$  (NB: different from growth pattern of components  $j$  in isolation) these can be plugged in formulas above to identify contributions to pro-poor growth of income components

## Dominance results (Duclos, 2009)

Duclos (Social Choice and Welfare, 2009) shows how classic first-order and second-order dominance results can be used to assess pro-poor growth robustly

In a nutshell, this involves assessing dominance using standard tools discussed earlier simple but after raising the second period poverty line by a reference fraction (proportionate approach – e.g., poverty line multiplied by growth rate of mean income) or by adding a nominal amount (absolute approach, e.g., by adding average income gains to the poverty line)

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## Recognizing group composition changes

One key feature of all approaches discussed thus far: **group composition changes are ignored**

We looked at change in poverty indices, at percentile growth, group incomes but there is mobility in the income distribution:

- ▶ people in poverty or at selected percentiles are not the same people over time
- ▶ people belong to different income groups at different period

Since different individuals are compared, such statistics can not be fully informative about **who** has gained from growth (and so whether, say, the people who were 'poor' at time  $t$  have gained more than those who were 'rich')

## Relaxing the 'anonymity' principle

The key principle that is binding here is the 'anonymity principle' according to which re-ordering people and incomes should not affect any poverty (or inequality) assessment

In the context of pro-poor growth assessments, support for such a principle is less obvious.

Let us now relax it. (Or more precisely replace it by a weaker principle that reshuffling people and their *vector of incomes* ( $y_0, y_1$ ) does not affect assessment.)

(Refs for this section: Jenkins & Van Kerm (2006,2011), Grimm (2007))

## Income growth profiles vs. Growth incidence curves

First, let  $\delta(x, y)$  measure the change in a person's income between base year income  $x$  and final year income  $y$ . For example,

- ▶  $\delta(x, y) = y - x$  (absolute income growth)
- ▶  $\delta(x, y) = \log y - \log x$  (proportionate income growth)

Then, rank individuals in increasing order of *initial period* income

# Income growth profiles vs. Growth incidence curves

*Growth incidence curve*

$$\{\delta(x^p, y^p); p\}$$

(where  $x^p$ ,  $y^p$  are  $p$ th quantiles)

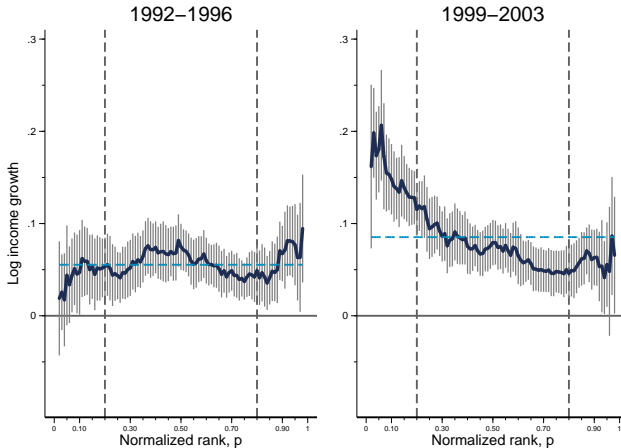
*Income growth profile*

$$\left\{ \int \delta(x^p, s) dF_{t+\tau}(s|x^p); p \right\}$$

where  $H$  is joint distribution of incomes at  $t$  and  $t + \tau$  and  $F_{t+\tau}$  is conditional distribution of  $t + \tau$  incomes given  $t$  income.

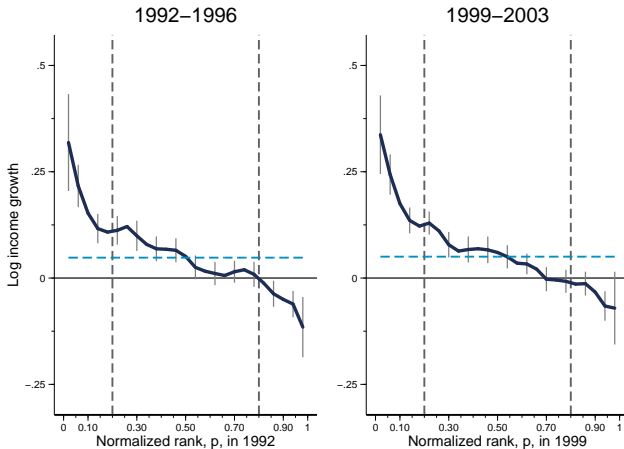
# Income growth profiles vs. Growth incidence curves

A GIC curve:



# Income growth profiles vs. Growth incidence curves

An income growth profile:



## Income growth profiles vs. Growth incidence curves

Interpretation of the shape of both GIC and IGP similar. The curves relate income growth to ranks in the initial distribution:

- ▶ A flat line indicates equi-distributed (distributionally-neutral) growth
- ▶ A downward sloping curve indicates a “pro-poor” growth pattern
- ▶ An upward sloping curve indicates a “pro-rich” growth pattern

But GIC about income ‘positions/groups’ whereas IGP is about incomes of named individuals

## Measurement error!

- ▶ IGP are much more sensitive to measurement error...
- ▶ Example of 'classical measurement error'
- ▶ Not much solutions
  - ▶ IV approach (but typically requires second measurements, e.g. other welfare measure or lagged info)
  - ▶ focus on accurately measured components only for comparison
  - ▶ improve collection as much as possible!

# Gini change decomposition

(Jenkins & Van Kerm, OEP 2006)

Change in Gini coefficient over time is a function of the difference between quantiles:

$$\text{GINI}(F_{t+\tau}; v) - \text{GINI}(F_t; v) = \int w(p; v) \left[ \frac{x^p}{\mu_t} - \frac{y^p}{\mu_{t+\tau}} \right] dp$$

This can be related to pro-poor growth pattern:

$$\text{GINI}(F_{t+\tau}; v) - \text{GINI}(F_t; v) = R(H; v) - P(H; v)$$

# Gini change decomposition

(Jenkins & Van Kerm, OEP 2006)

*Progressivity component:*

$$P(H; v) = \int w(F_t(x); v) \left[ \frac{y}{\mu_{t+\tau}} - \frac{x}{\mu_t} \right] dH(x, y)$$

$$w(p; v) = v(1 - p)^{v-1}$$

⇒ a measure of the 'pro-poorness' of growth

*Reranking component:*

$$R(H; v) = \int [w(F_t(x); v) - w(F_{t+\tau}(y); v)] \frac{y}{\mu_{t+\tau}} dH(x, y).$$

⇒ picks up the difference between GIC and IMP approaches

⇒ could be adapted to SST index decomposition in a straightforward manner

# Decomposition of additive poverty indices

(see Grimm 2007)

The change in an additive poverty index is the average of the change in the individual contributions:

$$P_1 - P_0 = \frac{1}{N} \sum_{i=1}^N \theta(y_{i1}, z) - \theta(y_{i0}, z)$$

Partition population by poverty status in the two periods: never poor, always poor, exiters, entrants

# Decomposition of additive poverty indices

(see Grimm 2007)

The change in poverty is equal to the contribution of the always poor plus the net effect of entrants and exiters

$$P_1 - P_0 = \frac{1}{N} \sum_{i=1}^N (\theta(y_{i1}, z) - \theta(y_{i0}, z))(y_{i0} < z \& y_{i1} < z) \quad (1)$$

$$+ \frac{1}{N} \sum_{i=1}^N (\theta(y_{i1}, z))(y_{i0} \geq z \& y_{i1} < z) \quad (2)$$

$$- \frac{1}{N} \sum_{i=1}^N (\theta(y_{i0}, z))(y_{i0} < z \& y_{i1} \geq z) \quad (3)$$

The gross change in poverty due to the **initially** poor is given by the first term (which can be negative or positive) and the third term (necessarily poverty-reducing).